

Solving linear simultaneous equations by elimination

A LEVEL LINKS

Scheme of work: 1c. Equations – quadratic/linear simultaneous

Key points

- Two equations are simultaneous when they are both true at the same time.
- Solving simultaneous linear equations in two unknowns involves finding the value of each unknown which works for both equations.
- Make sure that the coefficient of one of the unknowns is the same in both equations.
- Eliminate this equal unknown by either subtracting or adding the two equations.

Example 1 Solve the simultaneous equations $3x + y = 5$ and $x + y = 1$

$ \begin{array}{r} 3x + y = 5 \\ - \quad x + y = 1 \\ \hline 2x \quad = 4 \end{array} $ <p>So $x = 2$</p> <p>Using $x + y = 1$</p> $ \begin{array}{r} 2 + y = 1 \\ \hline y = -1 \end{array} $ <p>Check:</p> <table style="margin-left: 20px;"> <tr> <td>equation 1: $3 \times 2 + (-1) = 5$</td> <td>YES</td> </tr> <tr> <td>equation 2: $2 + (-1) = 1$</td> <td>YES</td> </tr> </table>	equation 1: $3 \times 2 + (-1) = 5$	YES	equation 2: $2 + (-1) = 1$	YES	<ol style="list-style-type: none"> 1 Subtract the second equation from the first equation to eliminate the y term. 2 To find the value of y, substitute $x = 2$ into one of the original equations. 3 Substitute the values of x and y into both equations to check your answers.
equation 1: $3 \times 2 + (-1) = 5$	YES				
equation 2: $2 + (-1) = 1$	YES				

Example 2 Solve $x + 2y = 13$ and $5x - 2y = 5$ simultaneously.

$ \begin{array}{r} x + 2y = 13 \\ + 5x - 2y = 5 \\ \hline 6x = 18 \end{array} $ <p>So $x = 3$</p> <p>Using $x + 2y = 13$ $3 + 2y = 13$ So $y = 5$</p> <p>Check: equation 1: $3 + 2 \times 5 = 13$ YES equation 2: $5 \times 3 - 2 \times 5 = 5$ YES</p>	<ol style="list-style-type: none"> 1 Add the two equations together to eliminate the y term. 2 To find the value of y, substitute $x = 3$ into one of the original equations. 3 Substitute the values of x and y into both equations to check your answers.
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Practice questions

Solve these simultaneous equations.

1 $4x + y = 8$
 $x + y = 5$

2 $3x + y = 7$
 $3x + 2y = 5$

3 $4x + y = 3$
 $3x - y = 11$

4 $3x + 4y = 7$
 $x - 4y = 5$

5 $2x + y = 11$
 $x - 3y = 9$

6 $2x + 3y = 11$
 $3x + 2y = 4$

7 $4x + y = 25$
 $x - 3y = 16$

Answers

1 $x = 1, y = 4$

2 $x = 3, y = -2$

3 $x = 2, y = -5$

4 $x = 3, y = -\frac{1}{2}$

5 $x = 6, y = -1$

6 $x = -2, y = 5$

7 $x = 7, y = -3$