

Non-linear simultaneous equations on graphs

A LEVEL LINKS

Scheme of work: 1c. Equations – quadratic/linear simultaneous

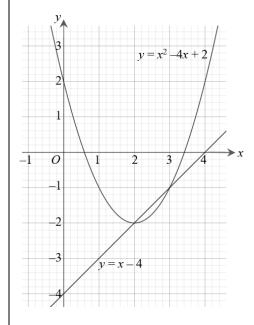
Key points

• You can solve any pair of simultaneous equations by drawing the graph of both equations and finding the point/points of intersection.

Example 1

Solve the simultaneous equations y = x - 4 and $y = x^2 - 4x + 2$ graphically.

x	0	1	2	3	4
y	2	-1	-2	-1	2



The line and curve intersect at x = 3, y = -1 and x = 2, y = -2

Check:

First equation
$$y = x - 4$$
:

$$-1 = 3 - 4$$
 YES
 $-2 = 2 - 4$ YES

Second equation
$$y = x^2 - 4x + 2$$
:

$$-1 = 3^2 - 4 \times 3 + 2$$

$$-2 = 2^2 - 4 \times 2 + 2$$

YES YES

- 1 Construct a table of values and calculate the points for the quadratic equation.
- 2 Plot the graph.
- 3 Plot the linear graph on the same grid using the gradient and *y*-intercept.
 - y = x 4 has gradient 1 and y-intercept -4.

- 4 The solutions of the simultaneous equations are the points of intersection.
- 5 Check your solutions by substituting the values into both equations.



Practice questions

1 Solve these pairs of simultaneous equations graphically.

a
$$y = x - 1$$
 and $y = x^2 - 4x + 3$

b
$$y = 1 - 3x$$
 and $y = x^2 - 3x - 3$

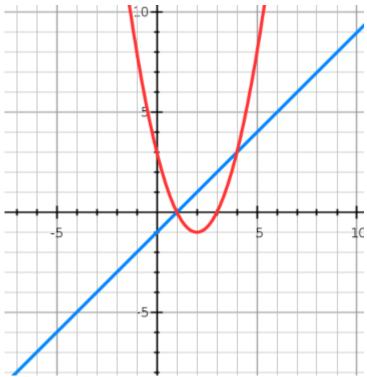
c
$$y = 3 - x$$
 and $y = x^2 + 2x + 5$

- 2 Solve the simultaneous equations x + y = 1 and $x^2 + y^2 = 25$ graphically.
- 3 a Solve the simultaneous equations 2x + y = 3 and $x^2 + y = 4$
 - i graphically
 - ii algebraically to 2 decimal places.
 - **b** Which method gives the more accurate solutions? Explain your answer.

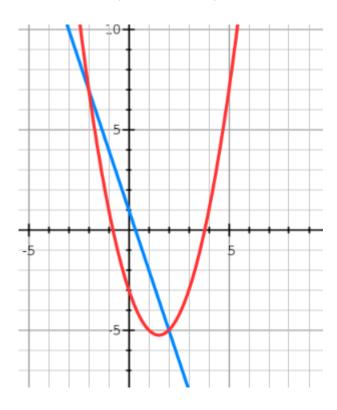


Answers

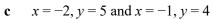
1 a
$$x = 1, y = 0 \text{ and } x = 4, y = 3$$

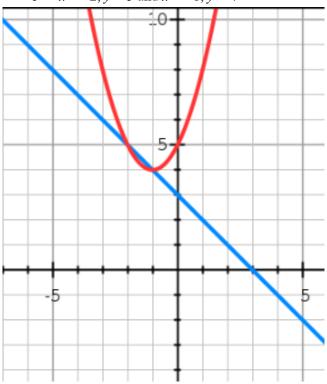


b
$$x = -2, y = 7 \text{ and } x = 2, y = -5$$

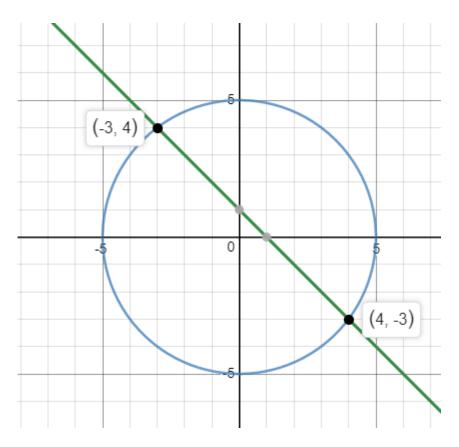






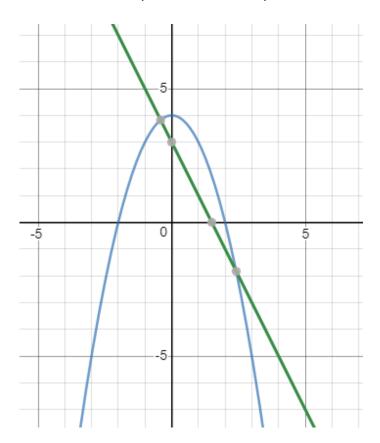


2
$$x = -3, y = 4 \text{ and } x = 4, y = -3$$

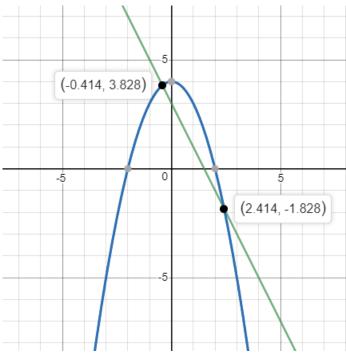




3 a i
$$x = 2.5, y = -2 \text{ and } x = -0.5, y = 4$$



ii
$$x = 2.41, y = -1.83$$
 and $x = -0.41, y = 3.83$



Solving algebraically gives the more accurate solutions as the solutions from the graph are only estimates, based on the accuracy of your graph.