



Translating graphs

A LEVEL LINKS

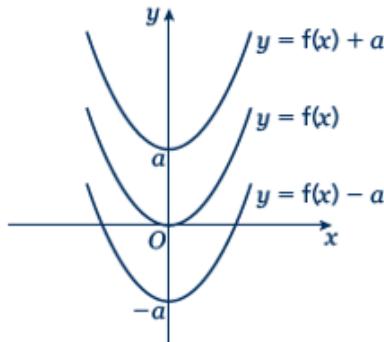
Scheme of work: 1f. Transformations – transforming graphs – $f(x)$ notation

Key points

- The transformation $y = f(x) \pm a$ is a translation of $y = f(x)$ parallel to the y -axis; it is a vertical translation.

As shown on the graph,

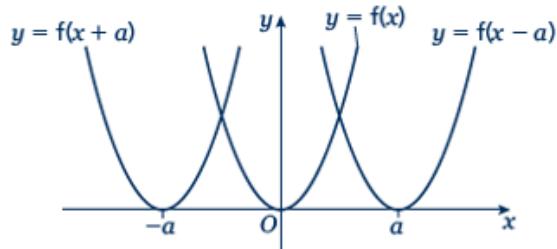
- $y = f(x) + a$ translates $y = f(x)$ up
- $y = f(x) - a$ translates $y = f(x)$ down.



- The transformation $y = f(x \pm a)$ is a translation of $y = f(x)$ parallel to the x -axis; it is a horizontal translation.

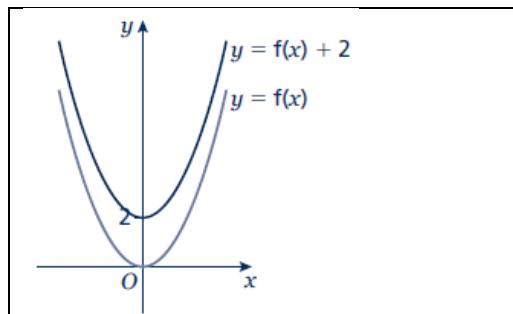
As shown on the graph,

- $y = f(x + a)$ translates $y = f(x)$ to the left
- $y = f(x - a)$ translates $y = f(x)$ to the right.



Example 1 The graph shows the function $y = f(x)$.

Sketch the graph of $y = f(x) + 2$.

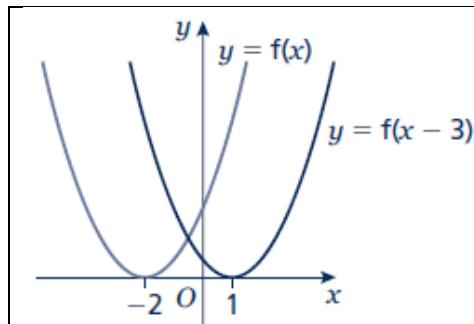
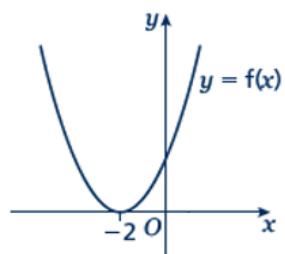


For the function $y = f(x) + 2$ translate the function $y = f(x)$ 2 units up.



Example 2 The graph shows the function $y = f(x)$.

Sketch the graph of $y = f(x - 3)$.



For the function $y = f(x - 3)$ translate the function $y = f(x)$ 3 units right.

Practice questions

1

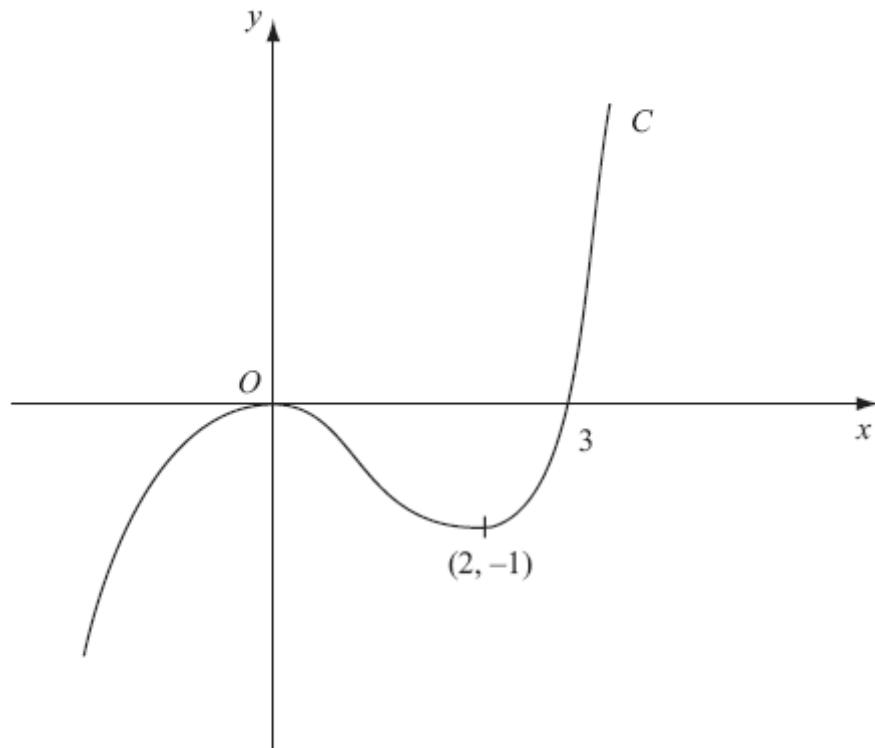


Figure 1

Figure 1 shows a sketch of the curve C with equation $y = f(x)$. There is a maximum at $(0, 0)$, a minimum at $(2, -1)$ and C passes through $(3, 0)$.

On separate diagrams, sketch the curve with equation

$$y = f(x + 3),$$

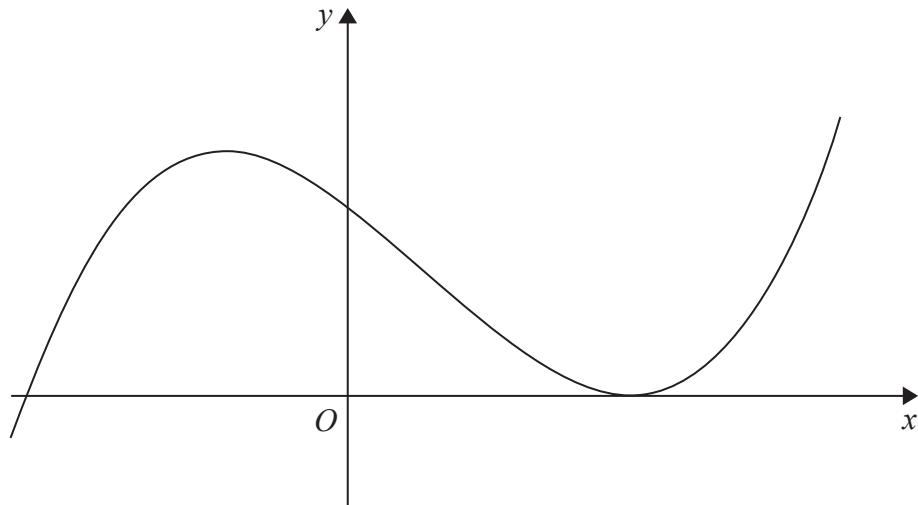

Figure 2

Figure 2 shows a sketch of part of the curve $y = f(x)$, $x \in \mathbb{R}$, where

$$f(x) = (2x - 5)^2(x + 3)$$

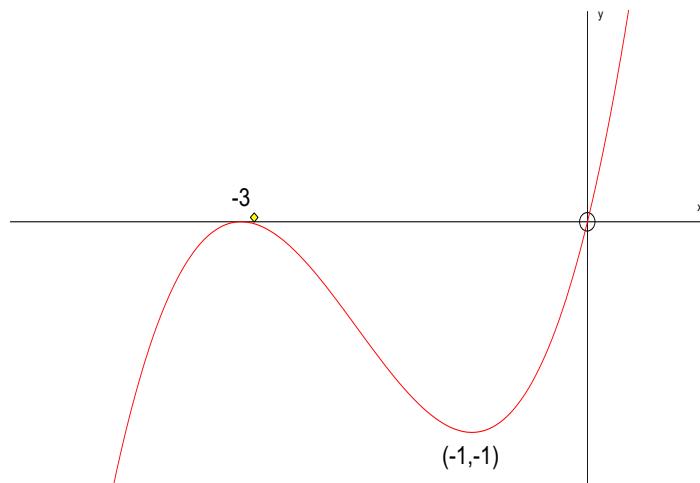
(a) Given that

- (i) the curve with equation $y = f(x) - k$, $x \in \mathbb{R}$, passes through the origin, find the value of the constant k ,
- (ii) the curve with equation $y = f(x + c)$, $x \in \mathbb{R}$, has a minimum point at the origin, find the value of the constant c .

(3)

Answers

1



2 (a) (i) $k = (-5)^2 \times 3 = 75$

(ii) $c = \frac{5}{2}$ only