

# Translating graphs

## A LEVEL LINKS

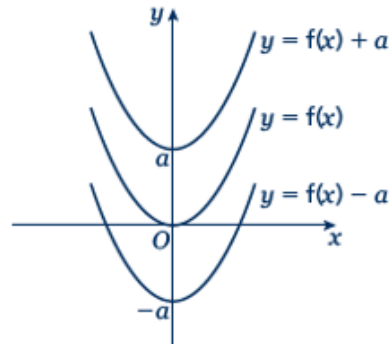
Scheme of work: 1f. Transformations – transforming graphs –  $f(x)$  notation

## Key points

- The transformation  $y = f(x) \pm a$  is a translation of  $y = f(x)$  parallel to the  $y$ -axis; it is a vertical translation.

As shown on the graph,

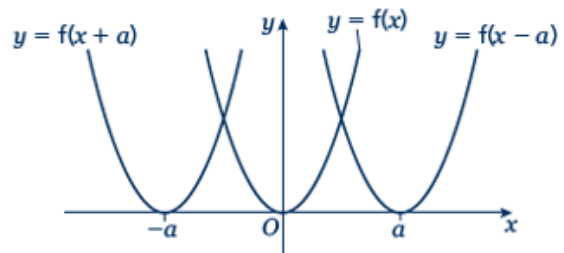
- $y = f(x) + a$  translates  $y = f(x)$  up
- $y = f(x) - a$  translates  $y = f(x)$  down.



- The transformation  $y = f(x \pm a)$  is a translation of  $y = f(x)$  parallel to the  $x$ -axis; it is a horizontal translation.

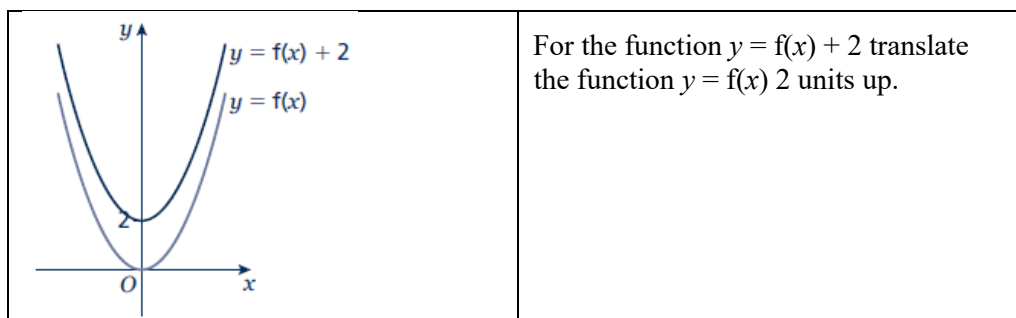
As shown on the graph,

- $y = f(x + a)$  translates  $y = f(x)$  to the left
- $y = f(x - a)$  translates  $y = f(x)$  to the right.



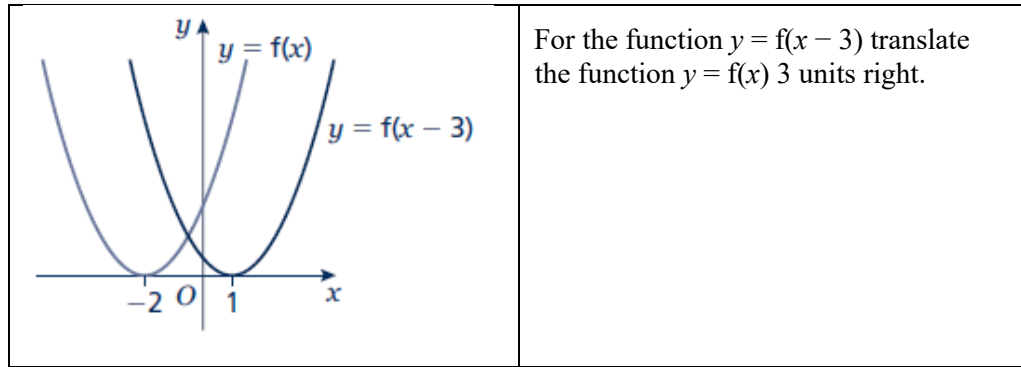
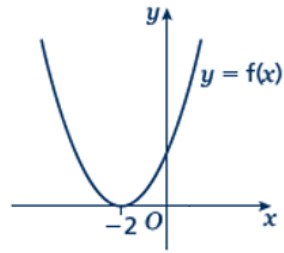
**Example 1** The graph shows the function  $y = f(x)$ .

Sketch the graph of  $y = f(x) + 2$ .



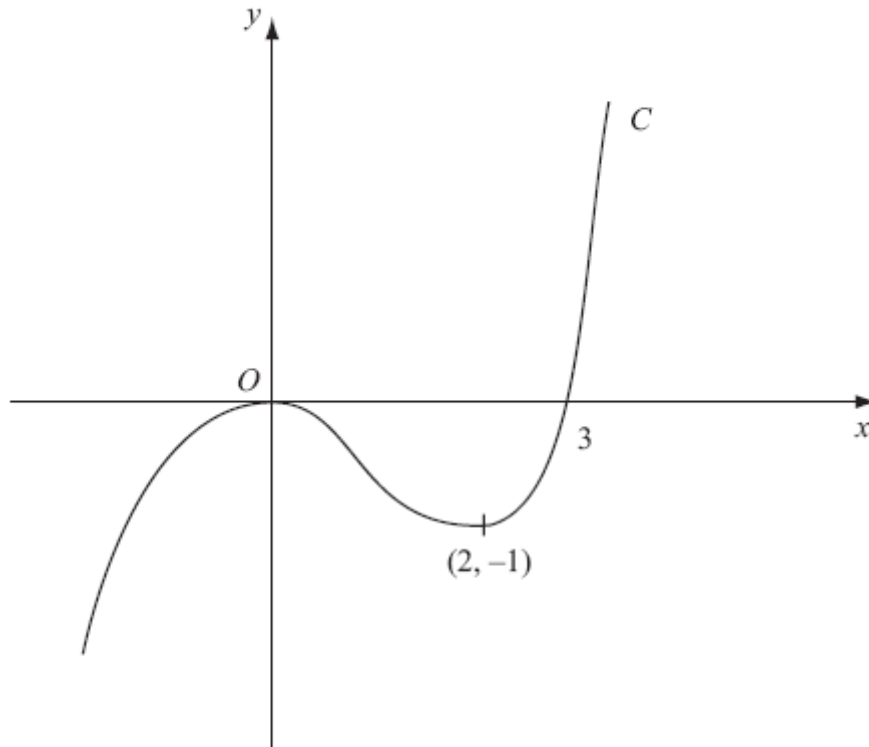
**Example 2** The graph shows the function  $y = f(x)$ .

Sketch the graph of  $y = f(x - 3)$ .



## Practice questions

1

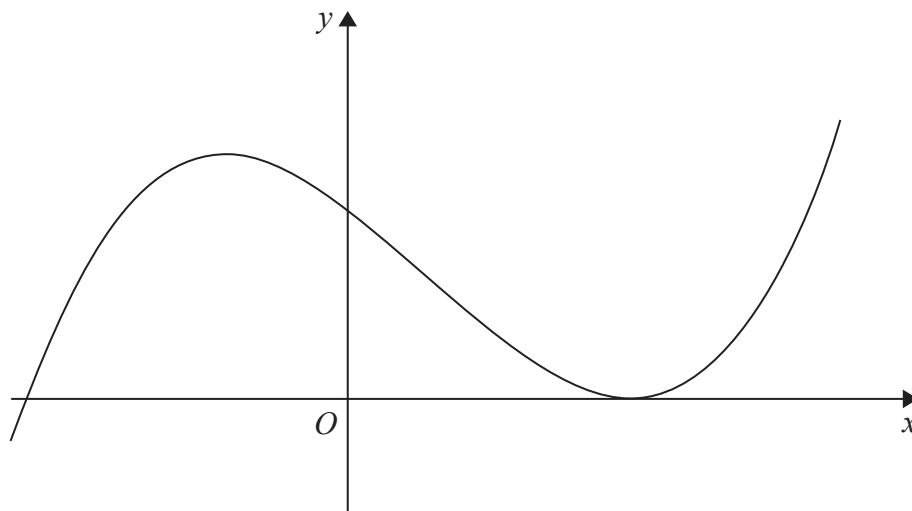


**Figure 1**

Figure 1 shows a sketch of the curve  $C$  with equation  $y = f(x)$ . There is a maximum at  $(0, 0)$ , a minimum at  $(2, -1)$  and  $C$  passes through  $(3, 0)$ .

On separate diagrams, sketch the curve with equation

$$y = f(x + 3),$$



**Figure 2**

Figure 2 shows a sketch of part of the curve  $y = f(x)$ ,  $x \in \mathbb{R}$ , where

$$f(x) = (2x - 5)^2 (x + 3)$$

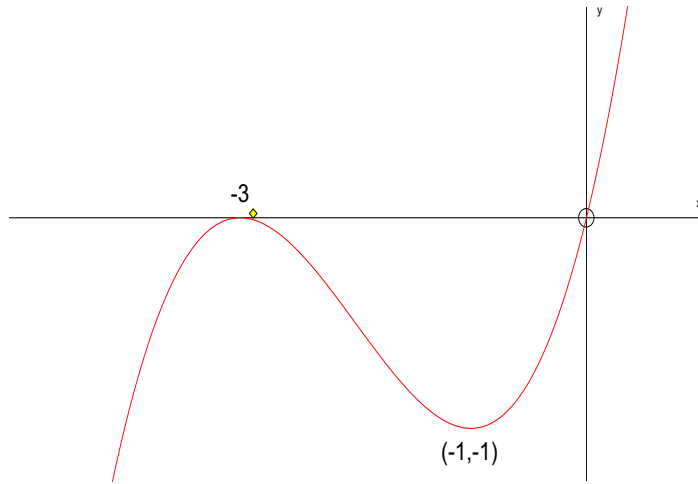
(a) Given that

- (i) the curve with equation  $y = f(x) - k$ ,  $x \in \mathbb{R}$ , passes through the origin, find the value of the constant  $k$ ,
- (ii) the curve with equation  $y = f(x + c)$ ,  $x \in \mathbb{R}$ , has a minimum point at the origin, find the value of the constant  $c$ .

**(3)**

## Answers

1



2 (a) (i)  $k = (-5)^2 \times 3 = 75$

(ii)  $c = \frac{5}{2}$  only