

# Gradients given two points

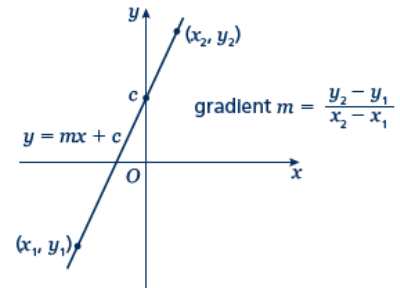
## A LEVEL LINKS

Scheme of work: 2a. Straight-line graphs, parallel/perpendicular, length and area problems

## Key points

- A straight line has the equation  $y = mx + c$ , where  $m$  is the gradient and  $c$  is the  $y$ -intercept (where  $x = 0$ ).
- The equation of a straight line can be written in the form  $ax + by + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers.
- When given the coordinates  $(x_1, y_1)$  and  $(x_2, y_2)$  of two points on a line the gradient is calculated using the

$$\text{formula } m = \frac{y_2 - y_1}{x_2 - x_1}$$



**Example 1** Work out the gradient of the line joining  $(2, 4)$  and  $(8, 7)$ .

$$x_1 = 2, x_2 = 8, y_1 = 4 \text{ and } y_2 = 7$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{7 - 4}{8 - 2} = \frac{3}{6} = \frac{1}{2}$$

$$m = \frac{1}{2}$$

Substitute the coordinates into the equation  $m = \frac{y_2 - y_1}{x_2 - x_1}$  to work out the gradient of the line.

## Practice questions

**1** Work out the gradient of the line joining each pair of coordinates.

**a**  $(4, 5), (10, 17)$

**b**  $(0, 6), (-4, 8)$

**c**  $(-1, -7), (5, 23)$

**d**  $(3, 10), (4, 7)$

## Answers

**1 a**  $m = 2$                       **b**  $m = -\frac{1}{2}$

**c**  $m = 5$                          **d**  $m = -3$