



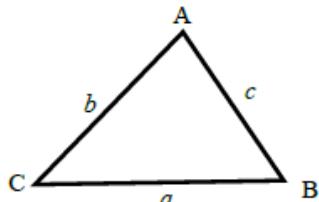
The cosine rule to find missing angles

A LEVEL LINKS

Scheme of work: 4a. Trigonometric ratios and graphs

Key points

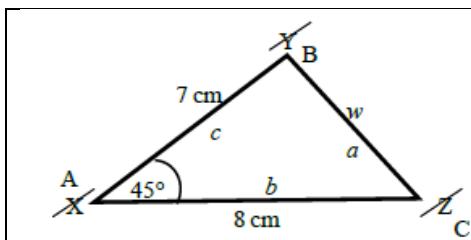
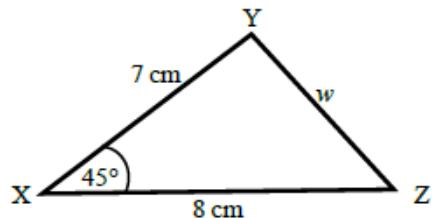
- a is the side opposite angle A.
- b is the side opposite angle B.
- c is the side opposite angle C.



- You can use the cosine rule to find the length of a side when two sides and the included angle are given.
- To calculate an unknown side use the formula $a^2 = b^2 + c^2 - 2bc \cos A$.
- Alternatively, you can use the cosine rule to find an unknown angle if the lengths of all three sides are given.
- To calculate an unknown angle use the formula $\cos A = \frac{b^2 + c^2 - a^2}{2bc}$.

Example 1 Work out the length of side w .

Give your answer correct to 3 significant figures.



$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$w^2 = 8^2 + 7^2 - 2 \times 8 \times 7 \times \cos 45^\circ$$

$$w^2 = 33.804\ 040\ 51\dots$$

$$w = \sqrt{33.804\ 040\ 51}$$

$$w = 5.81 \text{ cm}$$

1 Always start by labelling the angles and sides.

2 Write the cosine rule to find the side.

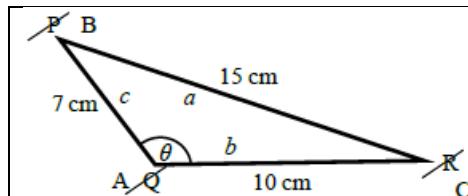
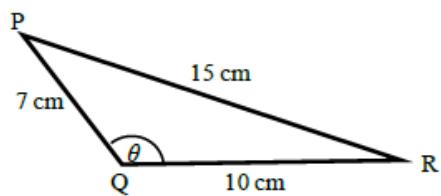
3 Substitute the values a , b and A into the formula.

4 Use a calculator to find w^2 and then w .

5 Round your final answer to 3 significant figures and write the units in your answer.



Example 2 Work out the size of angle θ .
Give your answer correct to 1 decimal place.



$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\cos \theta = \frac{10^2 + 7^2 - 15^2}{2 \times 10 \times 7}$$

$$\cos \theta = \frac{-76}{140}$$

$$\theta = 122.878\ 349\dots$$

$$\theta = 122.9^\circ$$

1 Always start by labelling the angles and sides.

2 Write the cosine rule to find the angle.

3 Substitute the values a , b and c into the formula.

4 Use \cos^{-1} to find the angle.

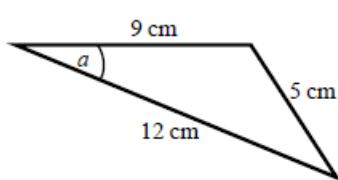
5 Use your calculator to work out $\cos^{-1}(-76 \div 140)$.

6 Round your answer to 1 decimal place and write the units in your answer.

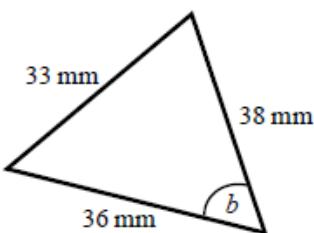
Practice questions

1 Calculate the angles labelled θ in each triangle.
Give your answer correct to 1 decimal place.

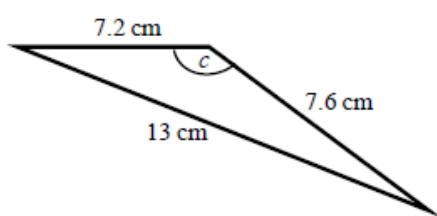
a



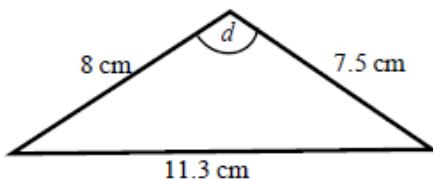
b



c



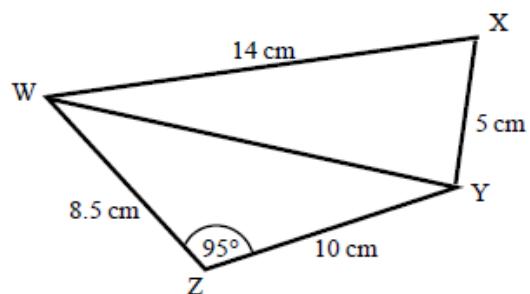
d





2 a Work out the length of WY.
Give your answer correct to
3 significant figures.

b Work out the size of angle WXY.
Give your answer correct to
1 decimal place.



Answers

1 a 22.2° b 52.9° c 122.9° d 93.6°

2 a 13.7 cm b 76.0°