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Treatment of syllabus content

P Digital resources

Metric equivalents

The language of mathematics

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