

Alan McSeveny Alan Parker Diane McSeveny-Foster Rachel McSeveny Bob Collard

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Content and Learning Specialist: Julian Lumb Project Manager: Shelly Wang Production Manager: Elizabeth Gosman & Aptara Editor: Aptara Designer: Anne Donald & Jennifer Johnston Cover Designer: Jennifer Johnston Desktop operator: Aptara Rights & Permissions Editor: Samantha Russell-Tulip Senior Publishing Services Analyst: Rob Curulli Cover art: Michael Barter Cover background: rf\_vector/shutterstock.com Illustrators: Michael Barter, Wendy Gorton, Nives Porcellato, Andrew Craig Printed in Malaysia

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Some of the images used in *Australian Signpost Maths 3* might have associations with deceased Indigenous Australians. Please be aware that these images might cause sadness or distress in Aboriginal or Torres Strait Islander communities.

## What is Australian Signpost Maths?

Australian Signpost Maths is a mathematics activity book series for students from Foundation to Year 6. The series has been written to meet the requirements of the Australian Curriculum.

The components of the series include Student Books, Teacher's Books, Mentals Books and an interactive Website. Teachers can select an appropriate program for every student from the rich and varied material provided.

The content has been carefully sequenced within each year level and across the series to take into account students' likely mathematical development.



## Structure of Australian Signpost Maths

Australian Signpost Maths emphasises the curriculum's syllabus content as well as problem-solving strategies, language development and the use of technology.

The syllabus is organised into three content strands and four proficiency strands:

### **Content Strands**

- Number and Algebra
- Measurement and Geometry
- Statistics and Probability
- Proficiency Strands (see page iv)
- Understanding
- Fluency
- Problem Solving
- Reasoning

The curriculum's **general capabilities** are developed throughout the Australian Signpost Maths program. These are:

- literacy
- numeracy
- information and communication technologies (ICT)
- critical and creative thinking.

Australian Signpost Maths also provides opportunities to develop other general capabilities, such as personal and social competence and intercultural understanding.

The cross-curriculum dimensions of the syllabus – 'Aboriginal and Torres Strait Islander histories and cultures', 'Asia and Australia's engagement with Asia' and 'Sustainability' – are embedded in the program.



To maximise the benefits of the program, the Student Book, Teacher's Book, Mentals Book and Website should be used together.

The structure of the **Student Book** allows teachers to determine both the order and the extent of content covered. Strands are organised separately so that the teacher, not the Student Book, decides the content of the next lesson. However, a suggested term program (see page x of this book) and a detailed program (see the Teacher's Book and Website) are also provided.

The **Teacher's Book** also provides lesson plans for each page of the Student Book and blackline masters to assist teachers in implementing the program.

The **Mentals Book** mixes examples from all strands. It revises the content covered in the Student Book. Each content strand is thoroughly covered, with the proficiency strands incorporated within each section. A special feature woven throughout the Mentals Book is the tables program in the four operations.

The innovative **Website** help teachers to bring mathematics alive with technology. The website provides interactive maths tools, games and practice opportunities as well as relevant resource masters and worksheets for all year levels. These can be used for whole-class, smallgroup and individual learning. The website also includes **Concept Check-In** a new diagnostic screener.

Student Book pages are colour-coded by section.

Number and Algebra A

**Measurement and Geometry A** 

**Statistics and Probability** 

Number and Algebra B

Measurement and Geometry B

Answers

## Australian Curriculum Proficiency Strands

The proficiency strands of the Australian Curriculum describe how content is explored or developed – that is, the 'thinking and doing' of mathematics.

## Understanding

#### Learning the concepts

Students build a robust knowledge of adaptable and transferable mathematical concepts. They make connections between related concepts and progressively apply the familiar to develop new ideas. They develop an understanding of the relationship between the 'why' and the 'how' of mathematics.\*

Conceptual understanding of maths ideas includes the explanation of a concept using text and diagrams. This occurs throughout Australian Signpost Maths at the top of many pages and is indicated by the Concepts icon.

### Fluency

#### Using the concepts

Students develop skills in choosing appropriate procedures, carrying out procedures flexibly, accurately, efficiently and appropriately, and recalling factual knowledge and concepts readily.\*

The practice of maths skills to build fluency occurs on every page of Australian Signpost Maths.

## **Problem Solving**

# Applying concepts and strategies to develop solutions to problems

Students develop the ability to make choices, interpret, formulate, model and investigate problem situations, and communicate solutions effectively.\*

Problem solving provides opportunities for students to use strategies and skills such as investigating and questioning, to collaborate with others and to communicate their findings to different audiences. Such activities are often indicated throughout Australian Signpost Maths by the Activity and Investigation icons.

## Reasoning

#### **Coherent and logical thought**

Students develop an increasingly sophisticated capacity for logical thought and actions, such as analysing, proving, evaluating, explaining, inferring, justifying and generalising.\*

Students require opportunities to explain their mathematical thinking and can do so through both diagrams and written explanations. Reasoning questions are located throughout Australian Signpost Maths.

<sup>\*</sup> The Australian Curriculum: Mathematics, v8.3 - Content structure

## **Special Features of Australian Signpost Maths**

 Traffic Light system allows students to reflect on their work and highlight any units that they are having trouble understanding. They tick the red for



units they feel they still don't understand, and green for those they feel they understand fully.

- Exercises are **well graded**. New work is reinforced in the Mentals Book.
- **Answers** are supplied in the back of this book as well as in the Teacher's Book.
- **Concept Check-In** diagnostic screener (on the Website) provides a snapshot of the class' conceptual understandings to aid in classroom management. It also allows teachers to measure progress over time.
- The eight **Diagnostic Tests** (now also in the back of this book) allow the teacher to discover each student's strengths and weaknesses, and the cross-references direct students to the pages where that work is introduced. Answers are supplied in the Teacher's Book.

- The **Dictionary** at the beginning of this Student Book will help students to learn the language of mathematics.
- **ID Cards** (in the Mentals Book, Teacher's Book and Website) review the language of mathematics by asking students to identify common terms, shapes and symbols.
- Important rules and concepts are clearly highlighted.
- Worked examples and explanations are given throughout the Student Book where new ideas are introduced.
- The use of **colour** makes emphasis clear and is highly motivating.
- **Cartoons** give instruction and friendly advice.
- Interactive activities are provided on the website for whole-class, small-group and individual learning.

## **Australian Signpost Icons**

Signpost icons are used throughout the book as cues to the essential nature of exercises and activities, and as a guide to ways of engaging with them. These icons often indicate alternative or more concrete approaches to dealing with concepts.



This icon highlights **important rules and concepts** occurring throughout the book. It often appears with worked examples.



Activities provide **applications and enrichment**. These activities usually involve the use of concrete materials and partner or group work.



These enjoyable activities are used to **motivate and involve** students in mathematical pursuits. They usually involve games and puzzles.



Investigations allow students to **explore and discover** maths concepts.



This icon indicates the use of computers, calculators or other **information and communications technology**.

# **Contents and Syllabus Overview**

Suggested Program x
Contents Cross-reference x
Dictionary
Answers
Diagnostic Tests 178

3

KEY

Number and Algebra
Measurement and Geometry
Statistics and Probability

	N	umber and Algebra A	Sub-strand	Number and place value	Fractions and decimals	Patterns and algebra	Content	Counting and numeration	Place value	ions	Number patterns	Suggested progress
Page	Unit	Title	Sub	Numb value	<sup>-</sup> ract	atte	S	Cour	Place	Fractions	Num	Sug
1	1:01	Skip Counting							$\overline{\mathbf{O}}$			Term 1
2	1:02	Odd and Even Numbers										
3	1:02	Odd and Even Numbers					(					
4	1:04	Numbers to 1000									-	
5	1:05	Numbers to 1 000										
6	1:06	Counting										
7	1:07	Counting										
8	1:08	Numbers to 1000										T1, T2*
9	1:09	Numbers to 1 000										,
10	1:10	Fractions of a Whole					-					Term 2
11	1:11	Fractions of a Collection										_
12	1:12	Numbers to 10000										
13	1:13	Numbers to 10000										
14	1:14	Fractions										
15	1:15	Comparing Fractions										
16	1:16	Number Patterns										T3, T4*
17	1:17	Numbers to 10000										
18	1:18	Ordering Numbers										
19	1:19	Rounding										
20	1:20	Fractions										Term 3
21	1:21	Fractions in Our World										
22	1:22	Numbers to 10000										
23	1:23	Place Value to 10000										
24	1:24	Number Patterns										
25	1:25	What's the Rule?										
26	1:26	Expanded Notation										T5, T6*
27	1:27	Numbers to 10000										
28	1:28	Number Patterns										
29	1:29	Number Patterns										
30	1:30	Numbers to 10000										
31	1:31	Expanded Notation										
32	1:32	Numbers to 10000										Term 4
33	1:33	Place Value to 10000										
34	1:34	Numbers to 10000										T7, T8*
35	1:35	Making Number Patterns										
36	1:36	Rounding										

\* Suggested placement for Diagnostic Tests 1 to 8 (see the Teacher's Book).

•			Sub-strand	Number and place value	Money and financial mathematics	Patterns and algebra	ent	L	Subtraction	Multiplication	c	alue	Number patterns	ested
	N	lumber and Algebra B	qn	umbe Iue	oney ather	ttern	Content	Addition	btrac	ultipl	Division	Place value	admu	b B n
Page	Unit	Title	ง	NL val	ΣĔ	Pa	Ŭ	Ac	Su	ž	D	Pla	N	ر م
37	2:01	Australian Money												Tern
38	2:02	Addition and Subtraction Facts												
39	2:03	Strategies												
40	2:04	Number Facts, ×2												
41	2:05	Addition by Looking for 10s												
42	2:06	Patterns in Adding and Subtracting												
43	2:07	Patterns Involving Subtraction												
44	2:08	Number Facts, × 5, × 10												
45	2:09	Number Facts, $\times 1$ , $\times 0$												
46	2:10	Mental Strategies												T1,
47	2:11	Subtraction from 2-Digit Numbers												
48	2:12	Multiplication Facts												
49	2:13	Number Facts, ×3												Ter
50	2:14	Addition to 99, No Trading												
51	2:15	Addition to 99, No Trading												
52	2:16	Multiplication												
53	2:17	Number Facts, Multiplication												
54	2:18	Multiplication Facts												
55	2:19	Relating × and ÷												
56	2:20	Money												_
57	2:21	Shopping												ТЗ,
58	2:22	Relating Addition and Subtraction												
59	2:23													
60	2:24	5 1 5												
61	2:25													
	2:26	Change from \$2												_
63	2:27	Money												Ter
	2:28													
	2:29													
	2:30													
	2:31	Linking Multiplication and Division												
	2:32													
	2:33	Division Facts from Multiplication Facts												
	2:34													
	2:35													T5,
	2:36													-
	2:37	5												
	2:38													
	2:39		_											Te
	2:40	т. — — — — — — — — — — — — — — — — — — —												Ter
	2:41	Addition Involving Hundreds Subtraction to 999												
	2:42													
	2:43	Addition to 999												
	2:44	Checking Subtraction by Addition												
	2:45	Inverse Operations, × and ÷												77
	2:46	Counting Change												T7,
	2:47	Rounding to the Nearest 5c												
	2:48	Problem Solving				1								
	2:49	T								-				1

\* Suggested placement for Diagnostic Tests 1 to 8 (see the Teacher's Book).

vii



\*Suggested placement for Diagnostic Tests 1 to 8 (see the Teacher's Book).

Vİİİ

Measurement and Geometric reasoning     Alternation       2D Space     3D Space	Location Transformations	0	lgested gress
	LTa	Angles	Sug
120 4:01 Properties of 3D Objects	-		Term 1
121 4:02 Symmetry			
122 4:03 Properties of 3D Objects	-		
123 4:04 Symmetry in Our World			
124 4:05 Parallel and Perpendicular Lines			
125 4:06 Regular and Irregular Shapes			T1, T2*
127 4:08 Position and Giving Directions			Term 2
128 4:09 Shapes Revision			
129 4:10 Properties of 2D Shapes			
130 4:11 Investigating Angles			T3, T4*
131 4:12 Angles			
132 4:13 The Trapezium and Parallelogram			
133 4:14 Features of 2D Shapes			
134 4:15 Right Angles			Term 3
135 4:16 Angles			
136 4:17 Describing Position			
137 4:18 Pathways Between Places			T5, T6*
138 4:19 Investigating Prisms and Cylinders			Term 4
139 4:20 Investigating Pyramids			
140 4:21 Creating Maps			
141 4:22 Mazes			
142 4:23 Investigating Spheres			
143 4:24 3D Objects			
144 4:25 Properties of 2D Shapes			T7, T8*
145 4:26 Properties of 2D Shapes			
146 4:27 The Net of a Cube			

\*Suggested placement for Diagnostic Tests 1. to 8 (see the Teacher's Book).

Page	Sta Unit	tistics and Probability Title	Sub-strand	Chance	Data representation and interpretation	Content	Chance	Data investigation	Data representation	Suggested progress
147	5:01	Using Blocks in Graphs		-						Term 1
148	5:02	Tables and Graphs								
149	5:03	Tables and Graphs						-		T1, T2*
150	5:04	Chance								, .=
151	5:05	Predicting Outcomes								Term 2
152	5:06	Picture Graphs								T3, T4*
153	5:07	Making Graphs								
154	5:08	Reading Tables and Graphs								Term 3
155	5:09	Reading for Number								
156	5:10	Reading Picture Graphs								
157	5:11	Drawing Graphs								T5, T6*
158	5:12	Ordering Events								T7, T8*
159	5:13	Repeating an Experiment								Term 4

\*Suggested placement for Diagnostic Tests 1 to 8 (see the Teacher's Book).

## **Suggested Program**

	Weeks 1–10	Weeks 11–20	Weeks 21–30	Weeks 31-end	
Number and Algebra A	1:01–1:09	1:10–1:19	1:20–1:31	1:32–1:36	
Number and Algebra B	2:01–2:12	2:13–2:26	2:27–2:39	2:40–2:50	
Measurement and Geometry A	3:01–3:07	3:08–3:17	3:18–3:27	3:28–3:33	
Measurement and Geometry B	4:01–4:07	4:08–4:14	4:15–4:18	4:19–4:27	
Statistics and Probability	5:01–5:04	5:05–5:07	5:08–5:12	5:13	

It is assumed that there are 10 weeks in each term.

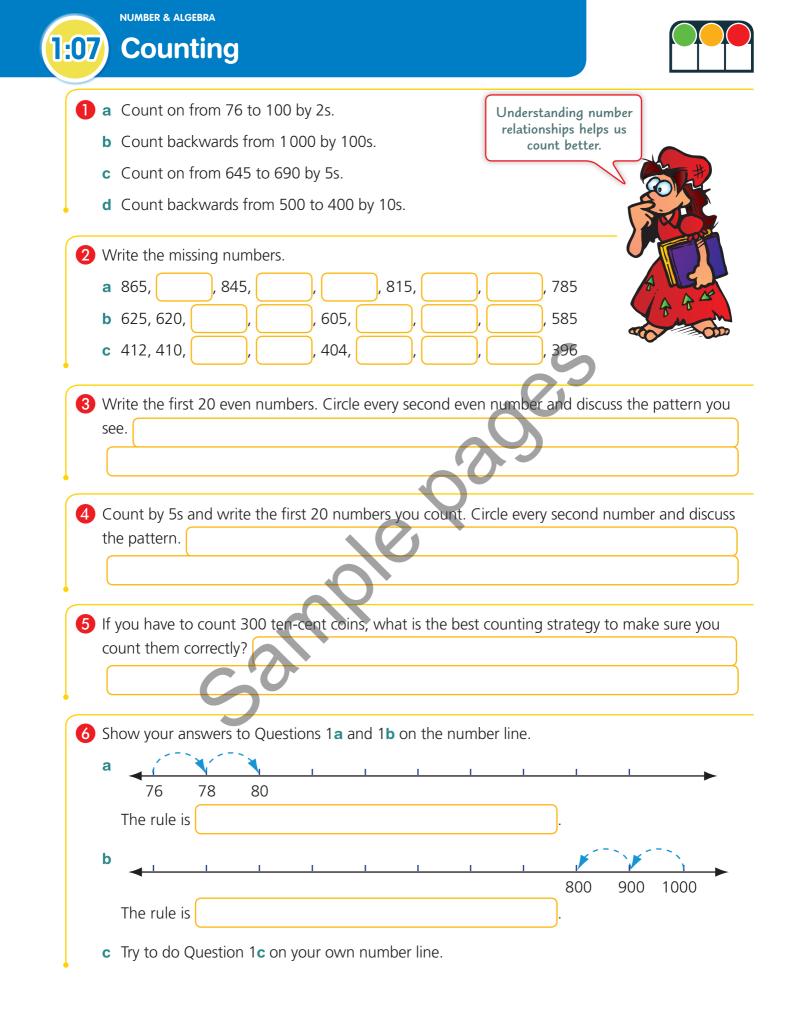
The eight Diagnostic Tests are found in the Teacher's Book.

See the Contents and Syllabus Overview on pages vi-ix for suggested placement of each test.

## **Contents Cross-reference**

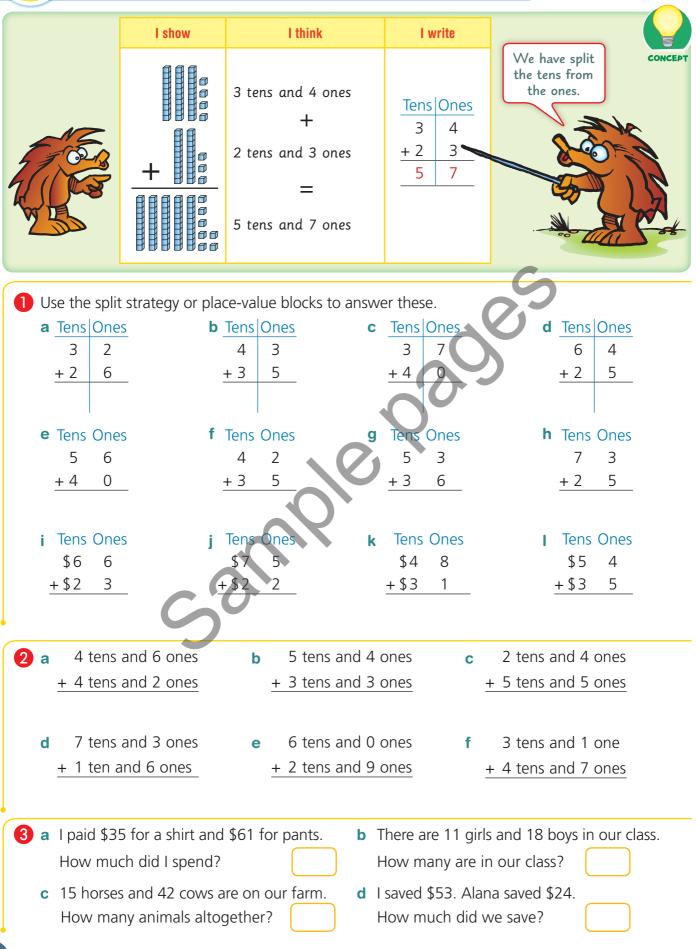
# Numbers and Algebra

1	Whole numbers	Pages	Australian Curriculum Reference 🔊
	Three-, four- and five-digit numbers and place value	4, 5, 6, 7, 8, 9, 12, 13, 17, 18, 22, 23, 26, 27, 30, 31, 32, 33, 34	Recognise, model, represent and order numbers to at least 10000 (ACMNA052); Apply place value to partition, rearrange and regroup numbers to at least 10 000 to assist calculations and solve problems (ACMNA053)
	Odd and even numbers	2, 3, 42	Investigate the conditions required for a number to be odd or even and identify odd and even numbers (ACMNA051); Describe, continue, and create number patterns resulting from performing addition or subtraction (ACMNA060)
	Rounding off	9, 19, 23, 36, 83	Recognise, model, represent and order numbers to at least 10000 (ACMNA052); Apply place value to partition, rearrange and regroup numbers to at least 10 000 to assist calculations and solve problems (ACMNA053); Represent money values in multiple ways and count the change required for simple transactions to the nearest five cents (ACMNA059)
2	Addition	Pages	Australian Curriculum Reference
	Mental strategies	36, 39, 41, 42, 46, 50, 58, 59, 63, 70, 71, 77, 79, 83	Apply place value to partition, rearrange and regroup numbers to at least 10 000 to assist calculations and solve problems (ACMNA053); Recognise and explain the connection between addition and subtraction (ACMNA054); Recall addition facts for single-digit numbers and related subtraction facts to develop increasingly efficient mental strategies for computation (ACMNA055); Represent money values in multiple ways and count the change required for simple transactions to the nearest five cents (ACMNA059); Describe, continue, and create number patterns resulting from performing addition or subtraction (ACMNA060)



# Addition to 99, No Trading

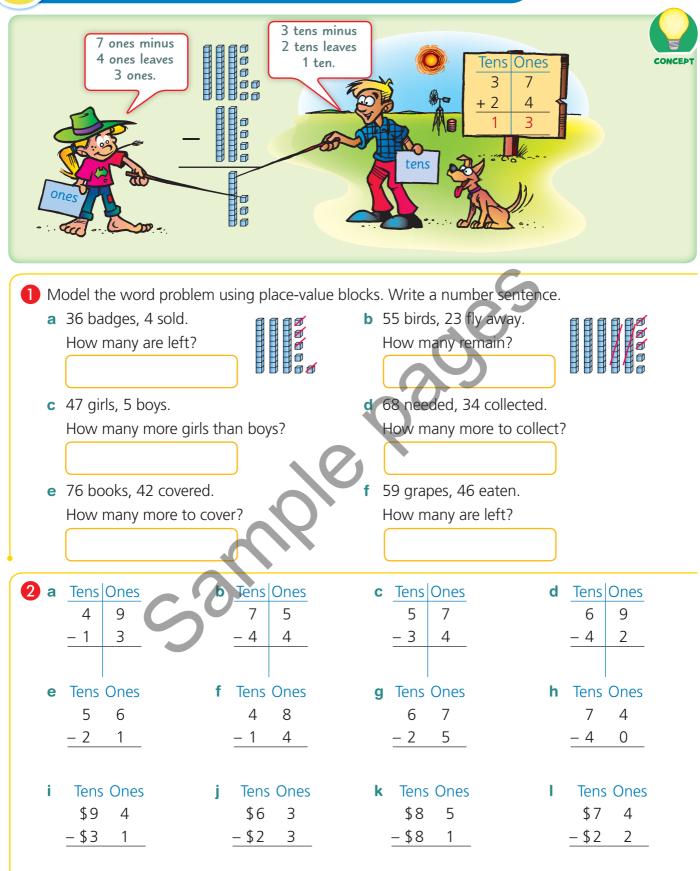






NUMBER & ALGEBRA





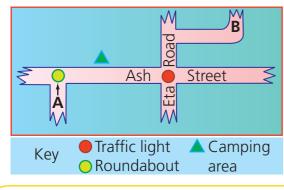
Use a calculator to check your answers in Question 2.

# Position and Giving Directions



A map gives us a view from above.

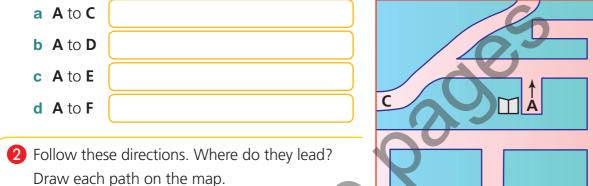
**MEASUREMENT & GEOMETRY** 





To get from A to B you turn right, then the first left, then the first right.

Write directions to get from place to place.



- a Start at **A**. Turn right, then the first right, then the second left.
- **b** Start at **A**. Turn right, then the first right, then the first right, then the first left, then the first right.

D

B

B

B

B

C

C

A

E

E

F

E

H

G

Key 
School

Hospital
Post office

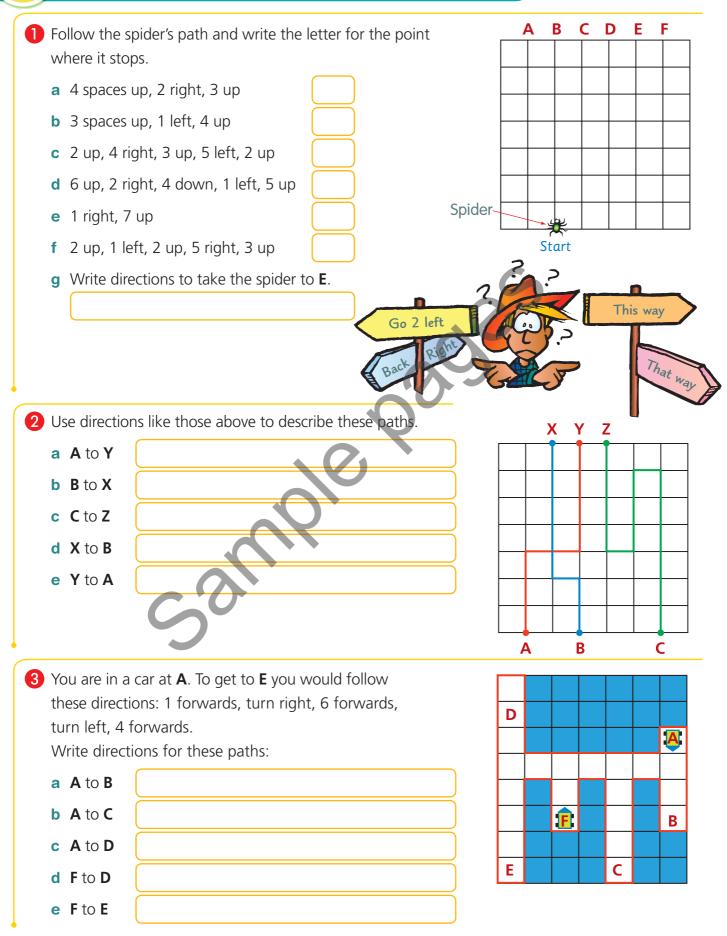
- **3** a Jenna is sitting in seat **J**. She moves two seats to the right, then one seat forwards. Where is she now?
  - **b** Patrick is sitting in seat **P**. He moves three seats to the left, then two seats forwards. Where is he now?
  - **c** Dmitri is sitting in seat **D**. He moves three seats backwards, then two seats to the left. Where is he now?
  - d Erin is sitting in seat **E**. She moves one seat to the right, then two seats backwards, then one seat left, then two seats forwards. Where is she now?

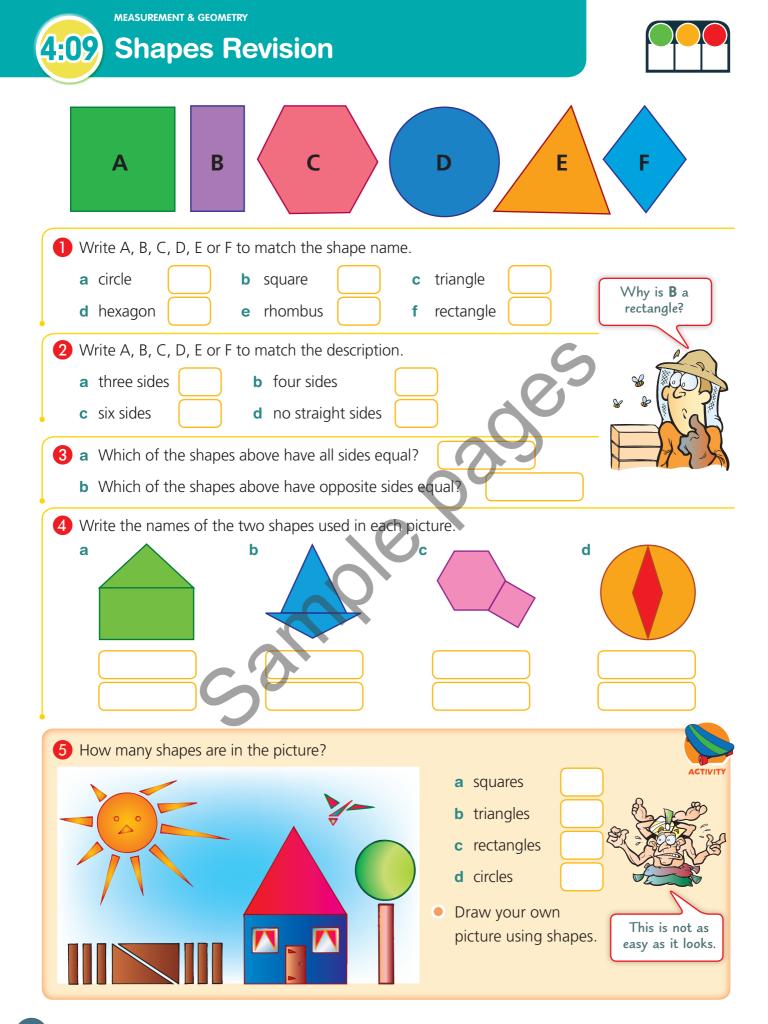
Classroom												
Τ	Forv	vards										
Α	В	С	D									
Ε	F	G	Η									
	J	K	L									
Μ	Ν	0	Ρ									

**MEASUREMENT & GEOMETRY** 

# **403** Position and Giving Directions







**4**81



Antonio's teacher made a **geoboard** like this by hammering nails into wood. Antonio used the geoboard to make shapes by stretching a rubber band over the nails.

。 。 。 。	· · · · · · · · · · · · · · · · · · ·	• • • • • • • •		0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	0 0 0 0	• • • • • • • • • • • • • • • • • • • •	0 0 0 0	• • • •	• • • •	0 0 0 0	0 0 0 0	0 0 0 0	I made those.
0	b H	low n low n low n	nany	nails	s wei	re us	ed to	o ma			-	e?	w ma	any s	Nur	nber of corners = nber of corners = on a square?
2	<ul> <li>a</li> <li>b</li> <li>V</li> <li>D</li> <li>c</li> <li>A</li> <li>D</li> <li>d</li> <li>D</li> </ul>	low n Vhat : Praw 1	e geo nany shap 3 of tagor a per a sha	boai side es ca then n has ntago pe o	rd ab s doo n yo n on s 5 si on o on th	oove, es ea ou dra the des n tha e geo	drav ach tr aw u geob How e geo oboa	w 3 t iang sing ooard y ma oboa	triang Jle ha 4 na d abo ny co ard.	gles ave? ails a ove. orne	of di s cor rs wo	ffere ners	nt sh	iape		d sizes. draw a pentagon?
			-			asked • •	d her Cut Disc Mix bac Use	frie you uss up k to you	nd to ir ow the s your geth	o ma vn so shap 5 pi er ag eces	ake a quare pes yo ieces gain. of pa	a pic e of p ou co anc	ture pape ut ou Lask	using r inte it.	g the o 5 p	the square back pieces. pieces. r to put the square