

NEW SENIOR

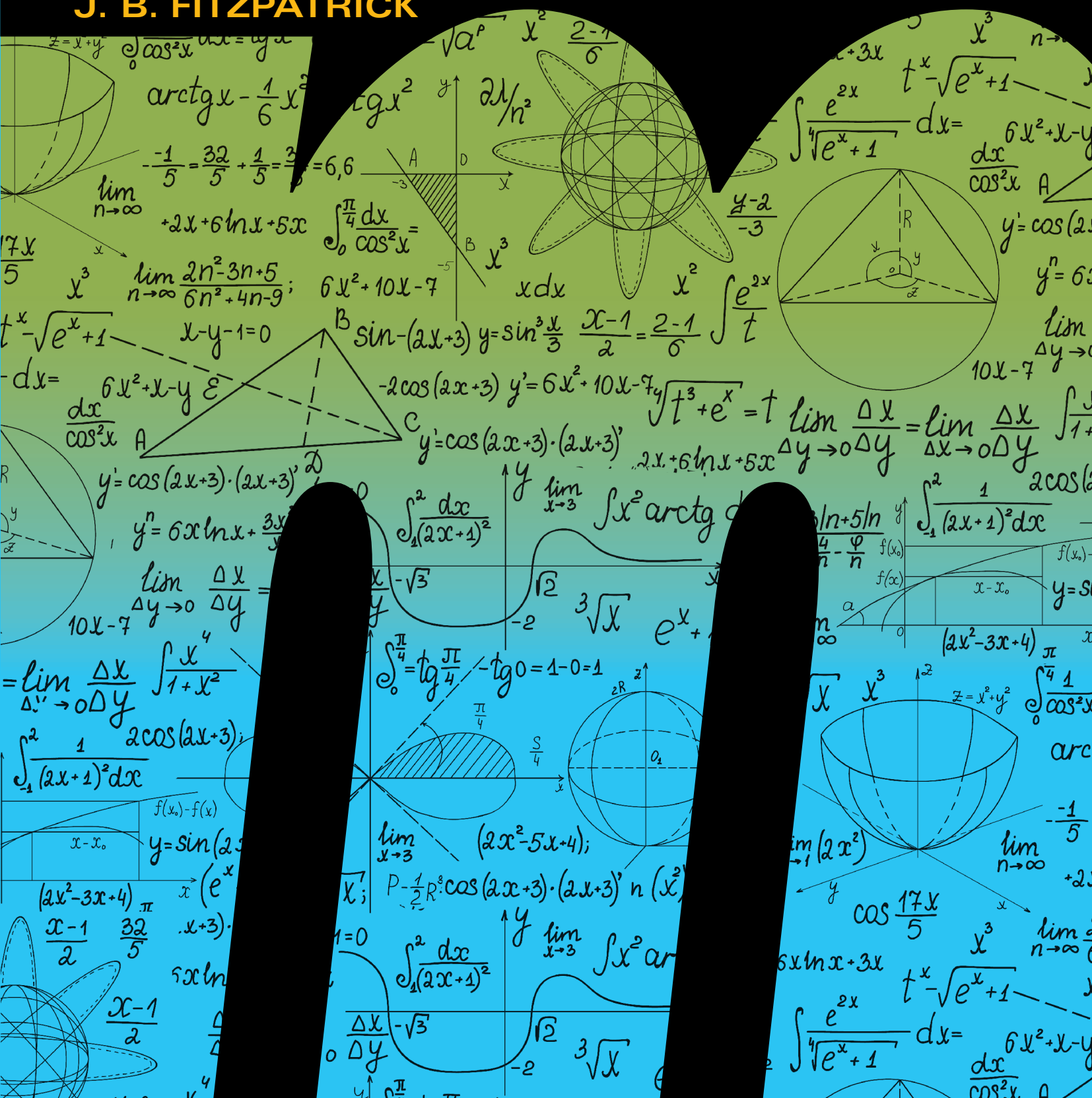
Mathematics

ADVANCED + EXTENSION 1 YEAR 12 | 4TH EDITION

BOB AUS

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NSW
STAGE 6



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