

NEW SENIOR

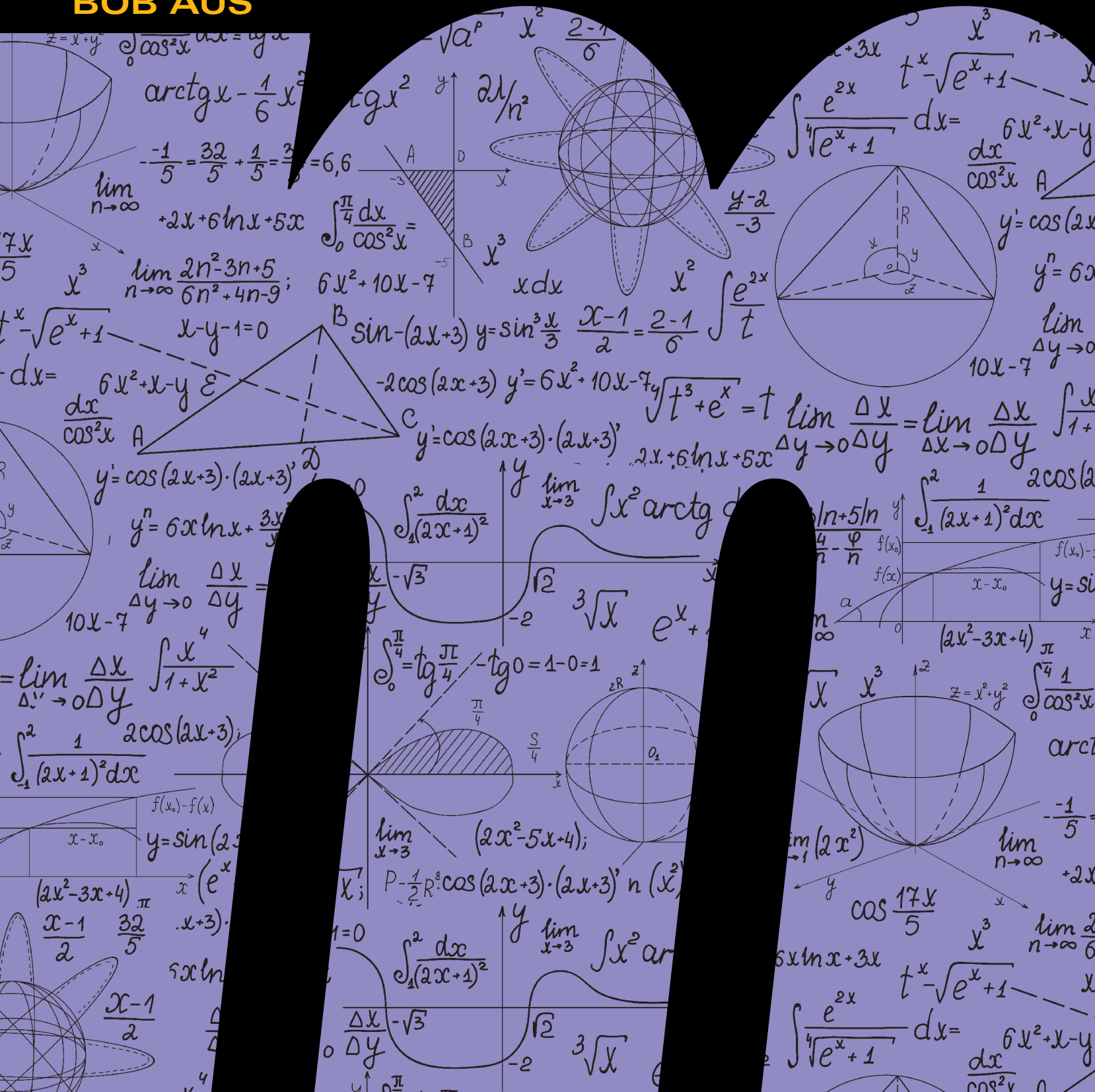
Mathematics

EXTENSION 2 YEAR 12 | 4TH EDITION

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BOB AUS

NSW
STAGE 6



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